Circle True or False. (1 point for correct answer, 0 if incorrect)

- 1. True False We can tell whether the midpoint rule approximating is an over or underestimating by looking at the first derivative.
- 2. True False Using Simpson's method will always give the exact answer when integrating a quadratic equation.

Show your work and justify your answers. Please circle or box your final answer.

3. (10 points) (a) (4 points) Approximate $\int_{-\pi}^{\pi} \cos(x) dx$ using the Trapezoid rule with n = 4 trapezoids. (Simplify your answer)

(b) (3 points) What is the maximum error in the previous estimation?

(c) (3 points) What is the smallest number of intervals n you need to use in order to guarantee that the trapezoid approximation of $\int_0^1 \frac{x^3}{6} dx$ is within $\frac{1}{12 \cdot 101}$.